

Speed-accuracy trade-off in Fitts' law tasks — On the equivalency of actual and nominal pointing precision

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ABSTRACT

Pointing tasks in human computer interaction obey certain speed-accuracy tradeoff rules. In general, the more accurate the task to be accomplished, the longer it takes, and vice versa. Fitts' law models the speed-accuracy tradeoff effect in pointing as imposed by the *task* parameters, through Fitts' index of difficulty (I_d) based on the ratio of the nominal movement distance and the size of the target. Operating with different speed or accuracy biases, performers may utilize more or less area than the target specifies, introducing another subjective layer of speed-accuracy tradeoff relative to the task specification. A conventional approach to overcome the impact of the subjective layer of speed-accuracy tradeoff is to use the *a posteriori* "effective" pointing precision W_e in lieu of the nominal target width W . Such an approach has lacked a theoretical or empirical foundation. This study investigates the nature and the relationship of the two layers of speed-accuracy tradeoff by systematically controlling both I_d and the index of target utilization I_u in a set of four experiments. Their results show that the impacts of the two layers of speed-accuracy tradeoff are not fundamentally equivalent. The use of W_e could indeed compensate for the difference in target utilization, but not completely. More logical Fitts' law parameter estimates can be obtained by the W_e adjustment, although its use also lowers the correlation between pointing time and the index of difficulty. The study also shows the complex interaction effect between I_d and I_u , suggesting that a simple and complete model accommodating both layers of speed-accuracy tradeoff may not exist.

Key words and phrases: Pointing, input, speed-accuracy tradeoff, Fitts' law, modeling, human performance.

1. Introduction

Acclaimed as one of the most successful human performance models (Newell, 1990), Fitts' law has served as one of the few quantitative foundations for human-computer interaction research. In particular, it has been used as a theoretical framework for computer input device evaluation (e.g. Card et al., 1978; ISO, 2000; MacKenzie, 1992), a tool for optimizing new interfaces (e.g. Lewis et al., 1992; MacKenzie and Zhang, 1999; Zhai et al., 2002), as well as a logical basis for modeling more complex human-computer interaction (HCI) tasks (Accot and Zhai, 1997). Fitts' law has also inspired alternative interaction techniques (e.g. Accot and Zhai, 2002; Kabbash and Buxton, 1995; Zhai et al., 1999) and gained new understandings, expansions, and applications in human-computer interaction research in recent years (e.g. Accot and Zhai, 2003; Guiard et al., 2001; McGuffin and Balakrishnan, 2002; Zhai et al., 2003).

Despite its impressive successes and critical importance, however, some of the fundamental issues in Fitts' law, either as a general human performance model or as a tool for human-computer interaction research, are still not fully understood in the literature. Speed-accuracy tradeoff is one of them.

In essence, Fitts' law is about revealing the rule of speed-accuracy¹ tradeoff in human control performance. As in many human-performed tasks, the more precisely the task is to be accomplished, the slower it is. Conversely, the faster the task is completed, the less precisely the task tends to be performed. For pointing tasks, Fitts' law precisely models how task precision affects pointing completion time:

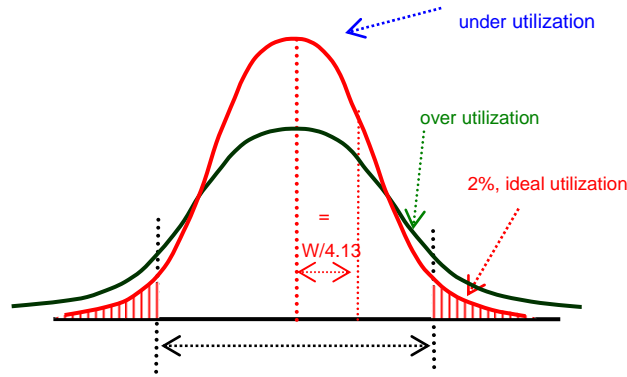
$$T = a + b \log_2 \left(\frac{D+W}{W} \right) \quad (1)$$

where a and b are constants reflecting the efficiency of the pointing system, D is the pointing distance, W is the target width and T is the mean (expected) time of task completion. In other words, Fitts' law formally models pointing speed (in the form of completion time T) as a function of relative task precision $W/(D+W)$. In Fitts' law task precision is quantified by an index of difficulty (I_d), which has several forms in the literature. Here we use the so-called Shannon formulation since it is the most logical one at the boundary condition $D = 0$ (MacKenzie, 1989):

$$I_d = \log_2 \left(\frac{D+W}{W} \right) \quad (2)$$

Note that so far the precision parameters, D and W , are *a priori* task parameters. In this sense the original Fitts' law is about the relationship of temporal (speed) performance and *task* precision. Ideally the human performer uses all of the precision tolerance (W) that the task specifies, no more, no less. Statistically, this means the spread of the endpoints (hits) of Fitts' aimed movements corresponds to the target width. For a Gaussian distribution, which the endpoints of a Fitts' law task are expected to form, the spread of endpoints can be measured by its standard deviation σ . Conventionally, the ideal case is that the central 96% of the endpoints (within $\sqrt{2\pi e}\sigma = 4.1325\sigma$) corresponds to W , i.e. $\sigma = W/4.1325$ (Figure 1).

¹ In many scientific fields, accuracy and precision are distinguished: accuracy refers to the nearness of a measurement to true value (a constant), and precision is the closeness of repeated measurements of the same quantity (dispersion). By such a distinction, precision would be a better term here, since Fitts' law is concerned with movement "resolution" (distance to width ratio). However, in the Fitts' law literature the term accuracy is conventionally used. Furthermore, it has not been of interest to Fitts' law research to study precise but inaccurate cases, namely, a group of trials repeatedly hitting a narrow band (precise) but off the center of the target (inaccurate). The dictionary definitions of the two terms are often interchangeable, and both are related to "exactness." In the rest of paper we do not distinguish these two terms, due to these considerations.



In actuality, either when performing laboratory experiments or when selecting graphical user interface (GUI) widgets on a computer with a mouse, the human performer (or the computer user in the context HCI) may or may not comply with the task precision as specified by W (Figure 1) – the width of the endpoints dispersion may depart from the target width W , causing either over or under utilization of the target area. In other words, the performer may introduce another layer of precision choice relative to the nominal task precision. The performer may be biased towards accuracy and use less area than the target gives, resulting in a more accurate than necessary but slower performance. Conversely, the performer may be biased towards speed and use more area than the target gives, resulting in a faster but more error prone performance. This second layer (or component) of speed-accuracy tradeoff is subjective and personal (hereafter referred as the subjective layer). In contrast, the bottom layer is objective (task specified) and nominal.

The existence of the subjective layer of accuracy complicates Fitts' law. Facing such a complication, students of Fitts' law have implicitly or explicitly taken two views. One is to continue to treat Fitts' law as a task model as in Equation 1 based on D and W , two nominal, *a priori*, and deterministic pointing task parameters. Alternatively, Fitts' law can be re-written based on actual behavioral parameters:

$$T = a + b \log_2 \left(\frac{D_e + W_e}{W_e} \right) \quad (3)$$

correspondingly,

$$I_{de} = \log_2 \left(\frac{D_e + W_e}{W_e} \right) \quad (4)$$

where,

$$W_e = 4.133\sigma \quad (5)$$

where D_e and W_e (or σ) are *a posteriori* and statistical measurement of the actual movements². As practiced in the literature, they are called effective distance and effective target width, although the implication of the term effective is a biased one without proof. For distinction, we refer Equation 1 as the task form of Fitts' law and Equation 3 as the behavior form of Fitts' law. One of the goals of the current study is to compare and contrast the two forms.

There are both practical and theoretical implications to each form. We will discuss the theoretical implications shortly. For practical purposes, particularly for work in HCI, the desirability of task vs. behavior form of Fitts' law isn't clear cut. Often it is desirable to relate a user's performance to the geometry of a graphical user interface. For example, for an interface designer it is important to know a user's average selection time as a function of task parameters such as a GUI widget in certain size and location. For another example, in Fitts' law based stylus keyboard optimization research researchers are concerned tapping time in relation to the geometrical variables – the relative location of keys (e.g. Lewis et al., 1992; MacKenzie and Zhang, 1999; Zhai et al., 2002). A task form of Fitts' law is more desired in these cases. On the other hand, it is logically difficult to expect Fitts' law in its task form to serve as a reliable tool in evaluating the performance of an input device characterized by a and b constants in Fitts' law (cf. Zhai, this issue) if the performer's actual pointing precision deviates too far from the specified task precision. In this case, it is reasonable to expect that Fitts' law in its behavioral form, or at least some modification of the task form of Fitts' law in consideration of the deviation, be more useful.

Instead of viewing the two forms as opposing models, a potentially more complete and more sophisticated approach is to represent the two layers, or two components, of speed-accuracy tradeoffs in one model. Such a model should relate time (or speed) to two independent factors, both concerning precision. The first is the task precision, as specified by target parameters D and W . The second independent factor is the degree of target area utilization the performer chooses. This is relative to the specified task precision and subjectively introduced by the performer. The performer may choose to be less precise than the task specification and use more area than W and hence gain a faster speed, or choose to be more precise than the task specification and use less area than W , causing a slower completion speed. Another goal of this study is to explore whether there exists a model of Fitts' law that explicitly relate time to both layers of speed-accuracy tradeoff.

The degree of target area utilization has to do with the risk of missing the target the performer is willing to take. A more risky behavior tends to result in a wider endpoints distribution and cause over-utilization of the target area. A more risk-averse behavior tends to result in a narrower endpoints distribution and cause under-utilization of the target area.

2. Theoretical and literature analysis

The possible mismatch between the actual pointing precision and the nominal task specification has long been realized by researchers (e.g. Crossman and Goodeve, 1983/1963; Fitts and Radford, 1966; Welford, 1968), but the topic has lacked rigorous treatment in the literature, effectively being kept “under the carpet”. The most common method of compensating for this mismatch to date relies on the behavioral form of Fitts' law. If the performer over- or under-utilized target width W , the *a posteriori* actual precision measured by 4.1325σ of the endpoints distribution, or W_e , would be used in lieu of nominal target width W . In the

² Since the difference of D vs. D_e is comparatively smaller than that of W vs. W_e , this study focuses on the latter.

Fitts' law literature (e.g. MacKenzie, 1991, section 2.4), the justification for the use of W_e is commonly traced to Welford (1968), which in turn attributes it to a report to the British Medical Research Council (MRC) by Crossman and Seymour in 1957. Based on Crossman and Goodeve (1983/1963), Crossman's Ph.D. thesis (Crossman, 1956) appears to be the earliest formal source of this formulation, although Fitts and Radford (1966) suggested that the use of effective width could even be traced back long before Fitts' law to Woodworth (1899). Crossman's reasoning of using W_e (Crossman, 1956), cited in Crossman and Goodeve (1983/1963), is as follows:

" I_d could be viewed as the difference between two more fundamental quantities, $\log_2 W$, measuring the entropy of the endpoint distribution and $\log_2(2A)^3$, measuring the entropy of a hypothetical initial distribution of motion amplitudes. Since, as noted by Fitts, endpoints are observed to be normally distributed about the center of the target, the theoretically correct expression for endpoint entropy $H(o)$, is: $H(o) = \log_2(2\pi e)^{1/2} \sigma_x$."

Some researchers of Fitts' law advocate W_e since "This adjustment lies at the very heart of the information-theoretic metaphor that movement amplitude area analogous to 'signals' and end-point variability (viz. target width) is analogous to 'noise'." (e.g. MacKenzie, 1991, section 2.4). This information-theoretic foundation, however, isn't very formal. First, the concepts of information in both Fitts' initial work (Fitts, 1954) and Crossman's reasoning, cited above, are more metaphorical than mathematical. Second, Crossman's logic based on a two-component analysis of I_d involving a separate entropy of "a hypothetical initial distribution of motion amplitudes" measured by $\log_2(2A)$, is a difficult one. Third, the information-theoretic account of Fitts' law, more specifically the analogy of signal transmission over a noisy channel (Shannon, 1948), is one among many competing theoretical explanations of Fitts' law (e.g. Crossman and Goodeve, 1983/1963; Keele, 1968; Meyer et al., 1988). In the same article by Crossman and Goodeve cited above, they concluded, "It seems difficult to develop a truly information derivation of Fitts' law" (p. 256) and went on to develop their control theory explanation of Fitts' law. Paul Fitts' own view on the theoretical basis of Fitts' law was not rigid. In their discussion of different indices of difficulty, Fitts and Peterson clearly stated, "Since neither index has been derived formally from a theory, choice between them should rest on heuristic considerations" (Fitts and Peterson, 1964, p. 111).

For clarity of notations, we hereafter denote the index of difficulty based on the *nominal* target width, as defined by Equation 2, I_{dn} , and use I_d as a generic reference to index of difficulty.

In practice, the use of I_{de} has been adopted by some, but not all, researchers. Conceptually the use of I_{de} requires the assumption that the actual behavioral precision and the nominal task precision in fact have the same impact: a reduction or expansion of actual endpoint dispersion W_e as a result of the performer's subjective bias is equivalent to the same amount of reduction or expansion of the nominal target width W . A compelling theoretical question here is whether *a posteriori* measurement is indeed cognitively, or quantitatively, equivalent to *a priori* task specification.

Empirically, there is a scarcity of evidence to prove or disprove whether and how well substituting I_{dn} with I_{de} could compensate for the influence of nominal and actual precision mismatch caused by the subjective layer of speed-accuracy tradeoff. It will be empirically informative to measure whether human performance adjusted with effective width is equivalent to the performance under a nominal width of the same size, had the performer complied with the exact target specification.

³ Due to its signal transmission analogy, the distance to target in Fitts' law, denoted as D in this paper, is also referred to as amplitude and denoted as A . Note also originally Fitts defined $I_d = \log_2(2A/W)$, hence Crossman's $\log_2(2A)$ here.

Aiming for the “standard” behavior of approximately 4% error rate, most Fitts' law studies instructed the participants to perform “as fast as possible and as accurately as possible,” but do not systematically vary or control experimental participants' actual precision relative to the nominal task precision; hence it is difficult to evaluate the influence of the subjective layer of speed-accuracy tradeoff and the correction effects using I_{de} . Fitts and Radford (1966) is a rare exception. They systematically manipulated three subjects' operational bias towards accuracy (A), neutrality (N), and speed (S), by means of monetary award and penalty at 1 cent per point. For example, to bias the subjects toward a speed performance, the points for fast and correct, slow and correct, fast and wrong, and slow and wrong were +1, -1/2, -1/8 and -1, respectively.

Fitts' thesis was that human information capacity in motor responses is relatively constant despite different experimental manipulations, so their paper did not focus on the effect of I_{de} correction. Based on the data provided in (Fitts and Radford, 1966), however, we could construct Table 1 summarizing the average (over three participants) Fitts' law parameters in two of their experiments, using both I_{dn} and I_{de} .

Regression coefficients	Bias	Experiment 1		Experiment 2	
		I_{dn} based	I_{de} based	I_{dn} based	I_{de} based
a (ms)	A	-114	-148	-13	-46
	N	-85	-103	-13	-37
	S	-52	-75	33	-22
b (ms/bit)	A	73	93	68	63
	N	66	83	66	60
	S	56	77	53	55

Table 1. Summary of (Fitts and Radford, 1966)

Table 1 shows that the experimental bias conditions yielded very different b (and a) values using I_{dn} . From condition A to condition S, b varied 30% and 28.3% in Experiments 1 and 2, respectively. Risk-averse operation (A) tended to increase b and risky operation (S) tended to decrease b . Using I_{de} , the b values converged, but not completely. b still varied 20.8 % and 14.5% in Experiments 1 and 2. The same trend was true for a – converging, but not completely. The use of I_{de} did not appear to be able to completely compensate for performers' biases. If it did, we would expect these parameters to converge to the ideal values.

However, Fitts' and Radford's study (1966) has several weaknesses as a foundation for understanding the two layers of speed-accuracy tradeoff in pointing. First, it was not targeted at this topic, so a more in-depth investigation based on their data is difficult. Second, the number of experimental participants was very small in their experiments. Third, the error rates (and hence the target area utilization levels) in the study were all very far from the expected 4%. For example, the error rates of the three bias conditions were 24%, 27% and 34%, respectively, in their Experiment 1. If the target utilization levels in Fitts and Radford (1966) were closer to the ideal and deviated to both the over and under utilization sides, the results could be different.

In a more recent systematic study of speed-accuracy tradeoff in aimed movements, Adam (1992) found that there was indeed a speed accuracy trade-off at the subjective level: given the same task constraints the performers either produced very accurate but slow movements or very fast but inaccurate movements, depending on the “objectives” of the performers in the accuracy-speed bias spectrum. Different from the current study, the focus of Adam's study was how these objectives influence the kinematic features of reciprocal aiming movements. For example, the accuracy group of performers had lower peak speed than

the speed group. In terms of Fitts' law modeling, Adam found that substituting nominal target width with effective width increased the percentage of time variance accounted by Fitts' law. Fitts' law modeling details, such as the performance parameters a and b , were not reported in the study. The direction (under or over utilization of the target constraint) and amount of subjective bias were not quantified. The main conclusion of Adam's study is that ambiguous task instructions, such as to move as quickly and accurately as possible, are vulnerable to different strategic interpretations varying from an emphasis on accuracy to an emphasis on speed (Adam, 1992).

The focus of this study is on the modeling aspects of speed-accuracy tradeoff in aimed movements. The first task of is to empirically evaluate the I_{de} based behavior form of Fitts' law, when the target utilization levels are controlled to both sides of the ideal case. For clarity and convenience, we first formally define the notation of target width utilization. It is logical to assume that movement time is a function of both nominal task difficulty as quantified by I_{dn} and the level of target width (over) utilization by the performer, as quantified by I_u . Without committing to a particular form of the function, we have:

$$T = f(I_{dn}, I_u) \quad (6)$$

where the index of target width (over) utilization I_u is formally defined as:

$$I_u = \log_2\left(\frac{W_e}{W}\right) \quad (7)$$

or

$$I_u = \log_2\left(\frac{4.133\sigma}{W}\right) \quad (8)$$

The logarithmic transformation here is merely for mathematical convenience and symmetry with I_d . The absolute value of I_u indicates the degree to which the actual spread of the endpoints departs from the specified target width. A positive I_u means the performer over utilizes the target width and misses the target (error) with more than 4% probability. A zero I_u means the performer perfectly utilizes all variability specified by the task, no more, no less, and the error rate is exactly 4%. A negative I_u means that the performer under utilizes the target area, leaving a certain amount of safety margin, and misses the target with less than 4% probability.

In order to thoroughly study speed-accuracy tradeoff in pointing, in particular whether the impact of a non-zero I_u is compensated by replacing the task form of Fitts' law $T = f(I_{dn})$ with a behavior form of Fitts' law $T = f(I_{de})$, empirical studies which systematically manipulate both index of difficulty I_{dn} and index of target utilization I_u have to be conducted.

3. Experiment 1

3.1 Set-up and design

Twelve volunteers, of different gender (9 male and 3 female) and age (21 to 38 years, mean 26), participated in a target pointing experiment on a tablet computer (FUJITSU FMV Stylistic) with a screen size of 21 cm x 15.6 cm. Each pixel on the screen was 0.2055 mm wide. Similar to Fitts' original experiment (Fitts, 1954), participants did reciprocal pointing on a pair of vertical strip targets with a stylus. The width (W) of the targets and the center-to-center distances (D) between the two strips were set at $W = 12, 36, 72$ pixels and $D = 120, 360, 840$ pixels. The order of the nine width and distance combinations was randomized. Twelve trials were presented in each W, D combination, with the first tap excluded in analysis. If tapped on the outside of the target, an auditory signal was played.

Each participant was instructed to repeat the experiment three times with different operating conditions biased toward accuracy or speed: accurate (A), neutral (N), and fast (F). They were instructed to tap the

targets “as accurately as possible” in Condition A, “as accurately as possible and as fast as possible” in Condition N, and “as fast as possible” in Condition F. The goal was to make the participants operate at different levels of target utilization.

The order of the A, N, F conditions was balanced by a Latin square pattern across the twelve participants.

3.2 Data processing and analysis

Occasionally, “accidental clicks” outside the general region of the target were registered, due to either the confusion of the participant, or instrument error. We used two simple and conservative rules to remove these “outliers” from further analysis to prevent their disproportional impact on modeling (Press et al., 1992). The first rule of removal was that the user hit the same target the trial started from or the user landed in the direction opposite to where the destination target was. This was determined by the distance between the hit point and the target center being greater than $D-W/2$. Twenty-five trials were removed by this rule. The second rule was that the distance of the endpoint to the target center was 8 times greater than the target size. Three additional trials were removed by the second rule. A total of 28 trials were removed by these two rules, constituting a small percentage of the total number of trials (3564).

3.3 The index of target utilization I_u

The instructions for the operating strategy in the three experimental conditions had an obvious impact on participants’ target utilization and error rate. The average error rate in the A, N, F conditions was 3.2%, 10% and 19.4%, respectively. These rates overall were higher than what we hoped. Ideally the error rate in the N condition would be around 4% and A and F conditions be on the two opposite sides.

A wide range of target utilization levels was taken in the experiment by the participants (Figure 2). I_u varied from -1 to 1.5 bit. Note that 1 bit of I_u change means that the spread of the endpoints is twice or half of the specified target width. The operating conditions (A, N, F) changed the overall I_u level. Furthermore, participants also shifted from target under utilization in low I_{dn} to target over utilization in high I_{dn} trials, regardless of the condition. Even under the N (neutral) condition, I_u was not maintained at the ideal level (zero bit). This could be a deliberate choice of strategy shift by the human performers, or it could be fundamentally difficult to maintain the same level of target utilization facing targets with different I_{dn} . Guiard (2002) explains the same effect from a power constraint vs. precision constraint perspective, albeit in different terminologies. Note also that the amount of shift caused by D and W change were not the same (Table 2).

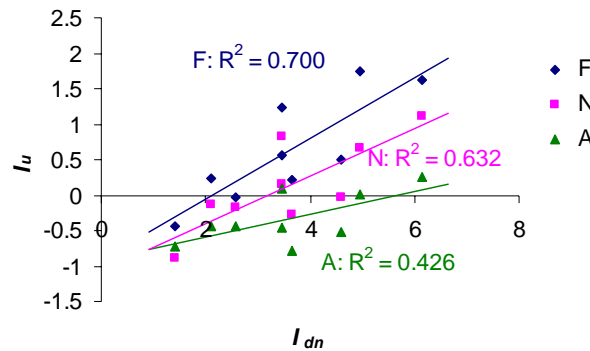


Figure 2. The index of target utilization I_u changes with instruction and I_{dn}

	Instruction Bias			
	A	N	F	Mean

D 120	-0.36	-0.07	0.34	-0.03
D 360	-0.30	0.21	0.76	0.23
D 840	-0.35	0.27	0.78	0.23
W 12	0.12	0.86	1.53	0.84
W 36	-0.47	-0.01	0.43	-0.02
W 72	-0.65	-0.44	-0.08	-0.39
Mean	-0.34	0.14	0.63	0.14

Table 2. Mean I_u values in different levels of D or W

3.4 The nominal I_{dn} model

As a baseline for further analysis, we first applied the basic task form of Fitts' law (Equation 1) to the data collected, using the task's nominal index of difficulty I_{dn} . The result is shown in Figure 3.

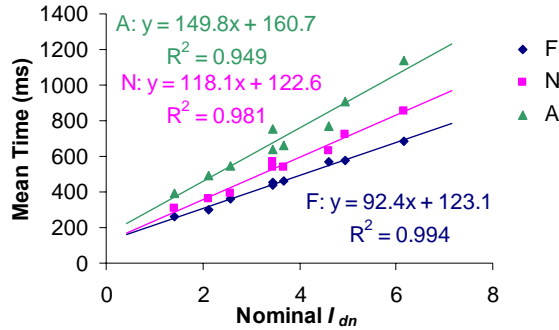


Figure 3. Linear regression T vs. I_{dn} in Experiment 1

When analyzed separately, within each operating condition T and I_{dn} correlated strongly. 95% to 99% of variance in T could be accounted for by the change of I_{dn} . There was a tendency that the more risky (faster-paced) the operating condition was, the stronger the correlation between T and I_{dn} was. The robustness of I_{dn} prediction here is quite remarkable given the very different operating biases (different levels of target width utilization) in these conditions. However, the coefficients of the regression results (or a and b in Equation 1) varied from one condition to another. Table 3 summarizes the results. The statistical significance levels (p , based on F tests) are also listed in italic font under each parameter, and the overall regression significance is listed under the r^2 value of the regression.

Strategy	a	b	r^2
A	160.7	149.8	0.949
<i>p</i> ($F_{1,7}$)	.013	<.0001	<.0001
N	122.6	118.1	0.981
<i>p</i> ($F_{1,7}$)	.001	<.0001	<.0001
F	123.1	92.4	0.994
<i>p</i> ($F_{1,7}$)	<.0001	<.0001	<.0001
Mixed	135.4	120.1	0.696
<i>p</i> ($F_{1,23}$)	.036	<.0001	<.0001

Table 3. Summary of T vs I_{dn} regression in Experiment 1

Results in Table 3 clearly shows that Fitts' law regression coefficients a and b using the I_{dn} model were influenced by the operating conditions (biases). b varied 62% from Condition F to A in this experiment.

If we perform the same Fitts' law regression based on the data from all conditions mixed, while still keeping the same unit of analysis 8 (I_{dn} levels) \times 3 (operating conditions), we obtain a much weaker correlation ($r^2 = 0.696$); see the last row of Table 3, although the correlation is still statistically significant.

3.5 The effective I_{de} model

We now test if the use of effective width, the behavior form of Fitts' law, would be able to compensate for the difference of operating conditions (strategy biases). The linear regression results between mean trial completion time T and the effective index of difficulty I_{de} are shown in Figure 4 and Table 4.

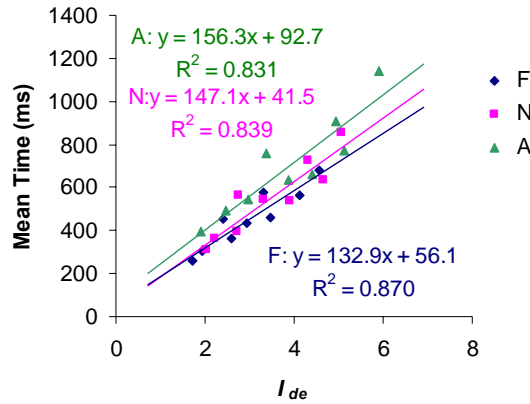


Figure 4. T vs. I_{de} regression in Experiment 1

Strategy	a	b	r^2
A	92.7	156.3	0.831
$p(F_{1,8})$.42	<.001	<.001
N	41.5	147.1	0.839
$p(F_{1,8})$.65	<.001	<.001
F	56.1	132.9	0.870
$p(F_{1,8})$.39	<.001	<.001
Mixed	13.2	161.0	0.825
$p(F_{1,25})$.81	<.0001	<.0001

Table 4. Summary of T vs. I_{de} regression in Experiment 1

Comparing Figure 3 vs. 4 and Table 3 vs. 4, the following observations can be made on the use of I_{de} .

First, the regression coefficients under different operating conditions were much closer to each other with I_{de} , showing the effect of compensation for the different levels of target utilization. The a values from different conditions were all reduced and the b values from different conditions became much closer to each other. From Conditions F to A, the b value's change was now 17.6% (in comparison to 62%).

Second, within each operating condition, r^2 between T and I_{de} decreased from the corresponding r^2 between T and I_{dn} . Only 83% to 87% of the T variance could be accounted for by I_{de} ⁴ (in comparison to 95% to 99% by I_{dn}). The same trend of r^2 reduction can be observed in the data of Fitts & Radford (1966). Why this was true will be discussed later. A counter example to this trend was seen in Mackenzie's recalculation of Fitts' 1954 data (MacKenzie, 1991, section 2.5 Table 2), which found a slight increase in r^2 by using I_{de} (from 0.983 to 0.99 and 0.98 to 0.988 respectively). Note that there the initial correlation was very high, and the change of correlation was small. Furthermore, since Fitts' 1954 data did not have endpoints location recordings, the recalculation of W_e was based on Z-score conversion from error rates – an imprecise or arbitrary estimation method when the error rate is low or zero.

Third, overall there was a shrinkage of the range of the independent variable from I_{dn} to I_{de} . Within the same condition, particularly for the more risky condition F, there was a counter-clockwise rotation of the regression line.

Fourth, if we use data from all operating conditions together, the r^2 value between T and I_{de} increased from the corresponding r^2 value between T and I_{dn} regression (0.723 to 0.825), showing a stronger regularity of $T = f(I_{de})$ than $T = f(I_{dn})$ in modeling pointing time in the presence of a wide range of target utilization.

In summary, the use of I_{de} demonstrated both benefits and drawbacks. It compensated operating biases (more converging a and b parameters), but not completely. Its robustness as a determinant of pointing time as measured by r^2 decreased within each operating condition but increased across conditions.

The utilization level in this experiment overall tilted to over utilization (positive I_u , see Figure 2). Even in Condition A, the overall error rate was 3.2%. It will be informative to also observe the more conservative under utilization side, as in the next experiment.

4. Experiment 2

The experiment had two operating conditions: A & F. In Condition F, the instruction was, “Move as fast as possible. It is okay if a few errors are made.” A gentle “ding” sound was played when an error was made. In Condition A, which in fact could be called the EA (extremely accurate) condition, participants were instructed to “Try to avoid any errors,” and a loud “ding” sound was played when a target was missed.

Eleven people of different gender (4 female and rest male) and age (20's to 50's), who had not been in the first experiment, participated in this experiment with both conditions. They were alternated between A to F and F to A order. An LCD display with stylus touch-sensitive surface (Wacom LCD Tablet Model PL-400) was used as the experiment apparatus. The rest of the experiment setup remained the same as Experiment 1.

Due to the quality of the tablet used in this experiment, many more erroneous trials were found. If the stylus struck the surface of the tablet too hard (and quickly bounced up), no click was registered. This meant the next click could be aimed at the “wrong” target. Using the same two rules outlined in Experiment 1, out of a total of 2178 trials in this experiment, 160 trials were removed by the first rule (tapped on the wrong side). Another 74 trials were removed by the second rule.

Under the instruction given in this experiment, participants indeed exhibited more conservative (risk-averse) behavior. Figure 5 shows the index of target utilization (cf. Figure 2). The I_u values at almost all I_{dn} levels were negative (the average error rates were 0 and 0.5% respectively for A and F conditions, see Table 6), but participants were clearly more conservative in Condition A than in Condition F. We tried to bias the participants in this experiment to the direction opposite to Experiment 1 that was overall on the risky side. Note that the operating condition labels (A, F, etc) are relative within each experiment.

⁴ Note that two $W:D$ combinations, 12:120 and 36:360, resulted in the same I_{dn} but different I_{de} due to the different amount of shift. The degrees of freedom in Table 3 and 4 were hence different.

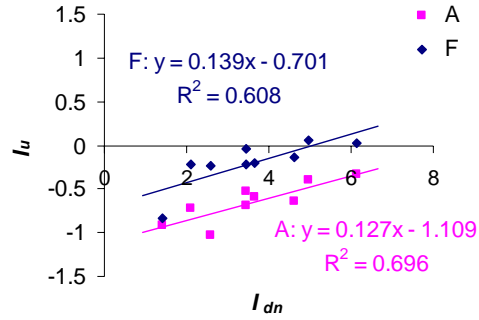


Figure 5. The index of target utilization I_u in Experiment 2

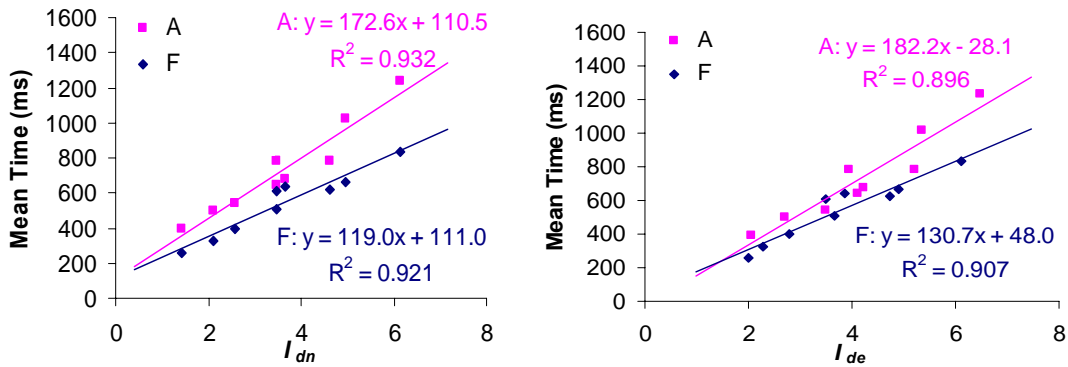


Figure 6. T vs. I_{dn} and T vs. I_{de} linear regressions results of Experiment 2

	Bias	a	b	r^2	p
$T = a + bI_d$	A	110.5	172.6	0.932	<.0001
	F	111.0	119.0	0.921	<.0001
	Mixed	110.8	145.8	0.747	<.0001
$T = a + bI_{de}$	A	-28.1	182.2	0.896	<.0001
	F	48.0	130.7	0.907	<.0001
	Mixed	-19.1	165.1	0.825	<.0001

Table 5. Fitts' law regression results of Experiment 2

Table 5 and Figure 6 show I_{dn} and I_{de} model regression results. Observations similar to those in Experiment 1 can be made here, but to a lesser degree: (1) As indicated by r^2 values I_{dn} is a (slightly) more robust pointing time determinant than I_{de} within each condition; (2) I_{de} is more robust than I_{dn} across conditions. (3) The range of I_{de} shrank from that of I_{dn} , but only from the low end of the index of difficulty this time. In fact for the A condition, the high end of I_{de} was further extended to the right. (4) I_{de} yielded more converging a and b parameters between the conditions than I_{dn} , hence it compensated for the different target utilization levels in different operating bias conditions (but not completely and to a lesser degree than in Experiment 1). Overall the changes caused by substituting I_{dn} with I_{de} are lesser in this experiment.

To verify the observations in these two experiments, we decided to conduct a more comprehensive experiment that covers a wide target utilization range on both sides.

5. Experiment 3

5.1 Set-up and design

Fifteen volunteers, 5 female and 10 male, aged 20 to 36 years old, participated in Experiment 3, in which the same experimental apparatus, software, and procedure as in Experiment 1 were used. The difference is that a greater range of target utilization is inducted: each participant was instructed to repeat the experiment five times with different operational strategies: extremely accurate (EA), accurate (A), neutral (N), fast (F) and extremely fast (EF). The following verbal instructions corresponding to each task were given by the experimenter to the participants: “Perform as accurately as possible and don’t worry about time or speed; try to avoid any error” in Condition EA; “as accurately as possible but keep some speed” in Condition A; “as accurately as possible and as fast as possible” in Condition N; “as fast as possible but keep some accuracy” in Condition F; and “as fast as possible and some errors are acceptable” in Condition EF.

5.2 Data processing and basic results

Similar to Experiments 1 and 2, 16 accidental trials were removed from the data pool out of a total of 7425 trials.

The error rates of the five conditions varied according to the verbal instructions, and the overall error rates in the EA, A, N, F, EF conditions were 0%, 1%, 4%, 9%, 22%, respectively, which were rather ideal because in condition N the error rate was at the standard 4% and the rest of the conditions were distributed symmetrically. As shown in Table 6, the overall I_u levels of the first two experiments were either tilted to positive (Experiment 1) or negative (Experiment 2). This experiment is similar to a combination of the first two.

Bias	Experiment 1			Experiment 2			Experiment 3		
	Error rate (%)	I_u max (bit)	I_u min (bit)	Error rate (%)	I_u max (bit)	I_u min (bit)	Error rate (%)	I_u max (bit)	I_u min (bit)
EA							0	-0.63	-1.33
A	3.2	0.24	-0.78	0	-0.33	-1.04	1	-0.17	-1.22
N	10	1.11	-0.88				4	0.23	-0.61
F	19.4	1.74	-0.44	0.5	-0.05	0.83	9	0.81	-0.73
EF							22	2.04	-0.59

Table 6. The I_u range and error rate in each operating condition of the first three experiments; the highlighted cell are the most neutral conditions in each experiment

The basic results of Experiment 3 with regard to the impacts of I_{de} vs. I_{dn} as the determinant of mean trial completion time are summarized in Figure 7 and Table 6. The results in this more comprehensive experiment verified the trends observed in the first two experiments. First, I_{dn} was once again shown to be a remarkably robust determinant of the mean pointing time within each condition. In spite of the very different instructions and hence the very different levels of overall target utilization, the r^2 values of T vs. I_{dn} linear regression were all above 0.9. There was a trend of increasing r^2 value from the more risk-averse conditions to the more risky conditions, consistent with the first two experiments. The r^2 values of T vs. I_{de} linear regression in each condition were uniformly lower than their corresponding r^2 values of T vs. I_{dn} in the same condition (Figure 7). Within the same operating condition, I_{dn} was clearly a stronger determinant of mean pointing time than I_{de} .

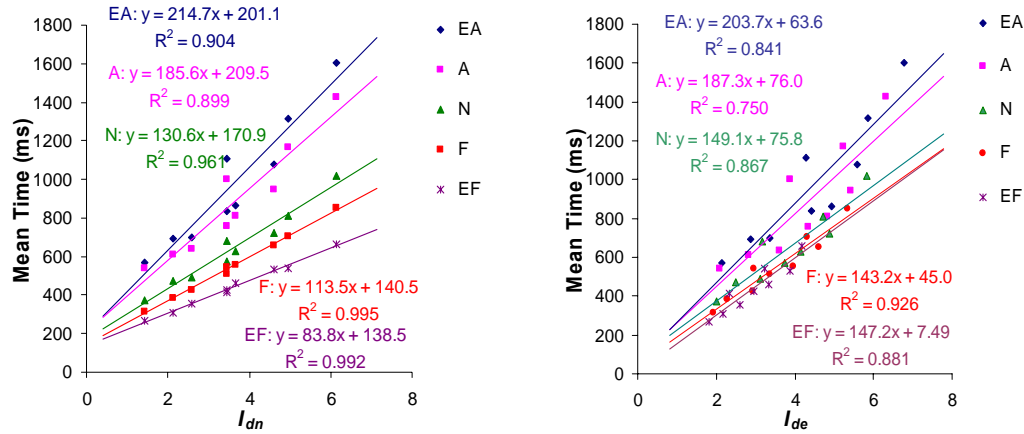


Figure 7. T vs. I_{dn} (left) and T vs. I_{de} (right) linear regression in Conditions EA, A, N, F and EF in Experiment 3

Tasks	Error (miss)	I_{dn} Model			I_{de} Model		
		a	b	r^2	a	b	r^2
EA	0 %	201.1	214.7	0.904	63.6	203.7	0.841
ρ		0.09	<0.0001	<0.0001	0.7	<0.001	<0.001
A	1 %	209.5	185.6	0.899	76.0	187.3	0.750
ρ		0.05	<0.0001	<0.0001	0.69	0.0025	0.0025
N	4 %	170.9	130.6	0.961	75.8	149.0	0.867
ρ		0.003	<0.0001	<0.0001	0.886	<0.001	<0.001
F	9 %	140.5	113.5	0.995	45.0	143.2	0.926
ρ		<0.0001	<0.0001	<0.0001	0.45	<0.0001	<0.0001
EF	22 %	138.5	83.8	0.992	7.49	147.2	0.881
ρ		<0.0001	<0.0001	<0.0001	0.90	<0.001	<0.001
Mixed		172.1	145.6	0.460	-92.4	207.5	0.783
ρ		0.07	<0.0001	<0.0001	0.17	<0.0001	<0.0001

Table 7. Summary of T vs. I_{dn} and T vs. I_{de} linear regression in Experiment 3

Second, in contrast to the strength of I_{dn} within each condition, I_{de} is a stronger determinant than I_{dn} when data from all conditions were merged in one regression. I_{de} accounted for 78% of the variance of mean trial completion time caused by both different levels of index of difficulty and the very different five operating strategies (See Figure 8). In comparison I_{dn} could account for only 46%. In this sense I_{de} clearly has the ability to convert some impact of the different levels of target utilization to index of difficulty.

Third, there was an overall rightward shift of I_{de} values from their corresponding I_{dn} values at the low (left) end of index of difficulty, but on the high end, the shift depended on the operating condition. For Condition

EF and F, the high end I_{de} points moved towards left, for Condition EA and A the high end I_{de} points actually further extended to the right, for condition N there was little change.

Fourth, and perhaps most strikingly, the regression lines of T vs. I_{de} were much closer across different conditions than those of T vs. I_{dn} , particularly for the more risky (faster) conditions (N, F, EF) (See Figure 7). The regression coefficients a and b hence were more converging between the conditions with I_{de} than with I_{dn} . Across the five conditions (from EA to FF), the a values were between 139 ms and 209 ms for the I_{dn} model and between 7.5 ms and 76 ms for the I_{de} model. The b values were between 83 ms/bit and 214 ms/bit (158% difference) for the I_{dn} model and between 143 ms/bit and 203 ms/bit (42% difference) for the I_{de} model. This also supports that I_{de} could at least partially overcome the different levels of target utilization due to operating biases and produce more stable estimates of Fitts' law coefficients.

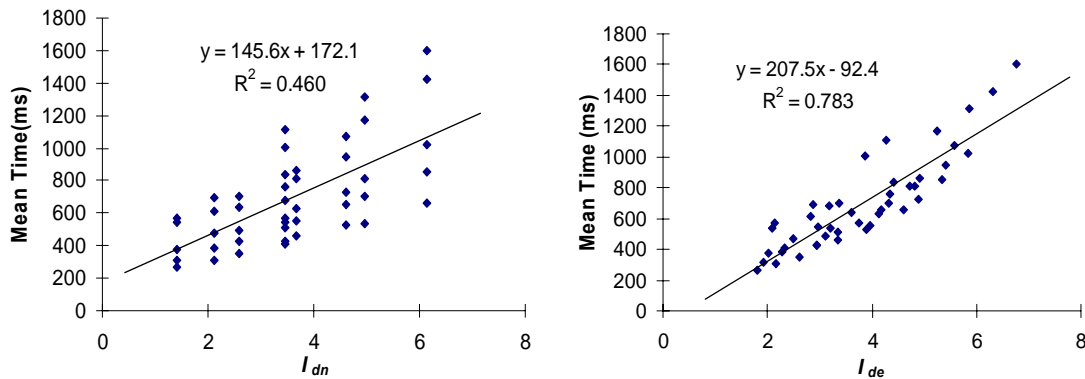


Figure 8. T vs. I_{dn} and T vs. I_{de} of all conditions combined

5.3 The interplay of I_u , I_{dn} , and W_e

We now examine the distribution of I_u , which is related to the third point above on the range and location of I_{de} shift. Figure 9 shows I_u across different I_{dn} values in each of the five conditions in Experiment 3. As a result of different operating conditions, target utilization levels as measured by I_u shifted up or down over a wide range (-1.33 to +2.04 bit) as a result of the instruction bias. Furthermore, I_u also changed with I_{dn} . While overall I_u was correlated with I_{dn} (the higher the I_{dn} , the higher the level of over utilization the participants tended to make), the degree of such a dependency changed with the operating condition. The more risky (faster-paced) the overall strategy was, the stronger the dependency was. In Condition EF the dependency was the strongest, with $r^2 = 0.831$. In Condition EA, in contrast, participants were quite consistently risk-averse, keeping I_u well below 0 across all I_{dn} values ($r^2 = 0.14$).

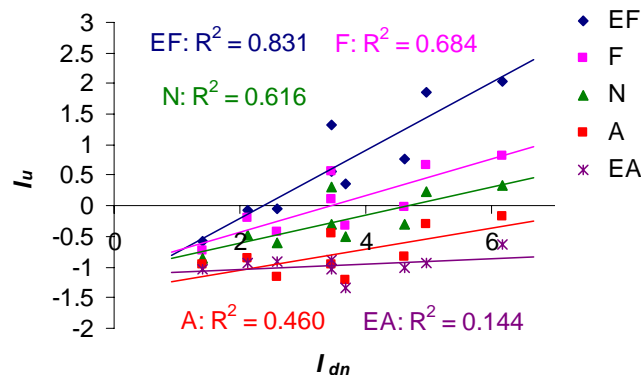


Figure 9. The index of target utilization I_u changes with instruction and I_{dn}

As we can see in Figure 9, even within the same operating condition and at the same I_{dn} level, I_u could still be very different. This leads us to examine the influence on I_u separately by W and D (Figure 10, see also Table 8). W was shown to have much stronger influence on I_u than D , as indicated by the slopes and r^2 values. This gives rise to an explanation of the fact that I_{de} was a weaker determinant than I_{dn} of completion time T within each condition. Since T and I_{dn} form a very strong correlation within each condition, any adjustment of I_d will only weaken the strength of the correlation, unless all I_d 's were changed with the same proportion. The I_{de} adjustment, however, depends on W_e (relative to W), which is influenced more by W than by D . This means the Fitts' law regression points at the same or similar I_{dn} , determined by $(D+W)/W$ ratio, may shift laterally to a different extent in I_{de} adjustment. Figure 11 shows the relative shifts in one experimental condition (N) of the regression points when I_{dn} (diamonds) is changed to I_{de} (squares).

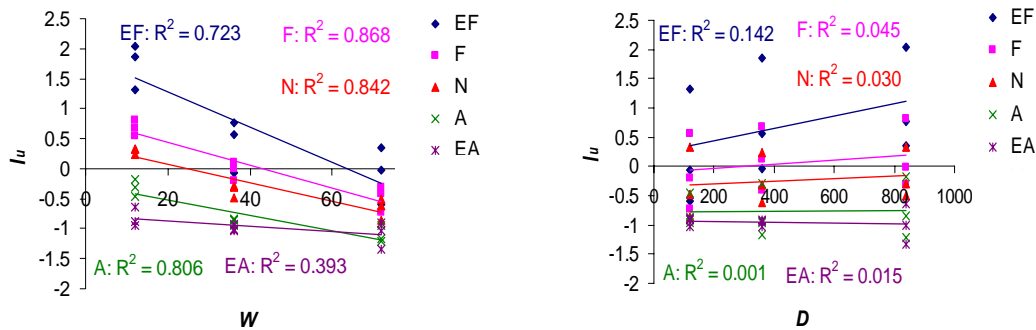


Figure 10. The index of target utilization I_u as a function of W (left), D (right), and instruction condition

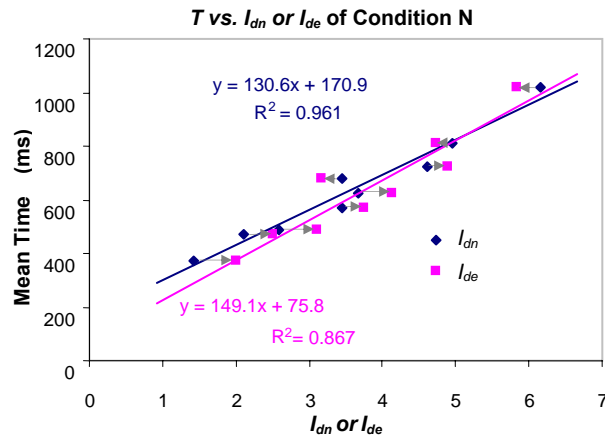


Figure 11. T vs. I_{dn} points (diamonds) shift different amount to T vs. I_{de} points (squares), causing lower correlation

Condition	W	12	36	72
	D			
EA	120	1.58	4.59	8.57
	360	1.52	4.27	9.28
	840	1.87	4.31	6.92

A	120	2.12	4.79	9.01
	360	2.36	4.50	7.77
	840	2.58	4.88	7.49
N	120	3.63	6.24	9.56
	360	3.41	7.02	11.40
	840	3.64	7.10	12.23
F	120	4.27	7.56	10.49
	360	4.61	9.41	13.07
	840	5.12	8.65	13.96
EF	120	7.27	8.33	11.59
	360	10.51	12.94	17.00
	840	11.94	14.75	22.34

Table 8. The standard deviation σ of endpoints at different D and W

Table 8 gives the standard deviation of the endpoints in Experiment 3 under different D and W values. When accuracy was emphasized, standard deviation was mostly decided by W . When accuracy was less emphasized, D began to exert impact on the standard deviation.

5.4 Preliminary conclusions of I_{dn} , I_{de} and the two layers of speed accuracy tradeoff

These three experiments systematically examined speed-accuracy tradeoffs in Fitts' pointing tasks. They showed that both the nominal task precision and performer's bias in over or under utilizing the given task precision tolerate change pointing completion time. The nominal index of difficulty I_{dn} is a remarkably robust predictor of completion time within each operating condition: the mean task completion time could be well accounted for by I_{dn} within each operating condition, even though the conditions were at very different overall levels of target utilization as quantified by I_u . The problem with the $T = f(I_{dn})$ model, however, is that the regression coefficients (a and b in Fitts' law) change with the overall level of I_u .

The experiments also showed that performers could rarely completely match the nominal task precision specification. I_u is not only affected by the performers' overall bias towards speed (over utilization of target) or accuracy (under utilization), it also interacts with I_{dn} . Higher I_{dn} tended to cause over utilization. Even if the performers overall operated at the standard error rate (4%), as in Condition N in Experiment 3, I_u still changed over 1 bit from low I_{dn} to high I_{dn} trials.

Overcoming some of the limitations of the $T = f(I_{dn})$ model, the $T = f(I_{de})$ model could compensate for some of the difference of I_u , particularly when the average I_u was around 0 or negative. As a result of using I_{de} the a and b estimates were much less affected by the operation conditions, and the r^2 value between T and I_{de} was much higher when both I_{dn} and I_u varied widely (data mixed from all conditions) than the r^2 value between T and I_{dn} (cf. Figure 7).

However, the correction effect of the I_{de} model is at the expense of a weakened T vs. I_d relationship. Within each operating bias condition, T vs. I_{de} consistently yielded lower r^2 than T vs. I_{dn} . This was partly due to the fact that the amount of shift from I_{dn} to I_{de} was influenced more by W than by D , so I_{dn} to I_{de} shifts were not always the same. Given the strong regularity of T vs. I_{dn} , any uneven change from I_{dn} would only result in a weaker regularity.

In sum, the behavioral model $T = f(I_{de})$ offers a compromise. It could absorb some of the mismatch between the nominal task specification and the performer's actual pointing precision, at the expense of a strong T vs.

I_d regularity. The results of T vs. I_{de} regression in terms of coefficients a and b were more stable than those of T vs. I_{dn} across operating biases, but they still did not completely converge. It appears that W_e as a *posteriori* adjustment does not fully account for the time performance difference caused by the second and subjective layer of speed-accuracy tradeoff — the performance's incomppliance with the task specification (a none-zero or varying I_u) resulting in an overall faster or slower speed.

6. Experiment 4

To observe more directly the exact extent of I_u impact on time performance, we conducted yet another experiment that systematically controlled effective width W_e and nominal target width W to a similar amount in two experimental conditions. If W_e could compensate I_u variance, we would expect the T vs. W_e relationship in the presence of varying I_u to be identical or similar to the T vs. W relationship when the performers obediently complied with the target size specification W with no or little I_u variance.

6.1 Set-up and experimental design

Ten volunteers, eight males and two females (averaging 24.2 years old), participated in this experiment. Some of them had participated in Experiment 1 or Experiment 2. The experiment was conducted on the same apparatus as in Experiments 1 and 3 with a similar experimental procedure. It consisted of two parts (or schemes): part A (“the target width incomplicant scheme”) and part B (“the target width compliant scheme”). In both parts, the participants performed reciprocal target tapping with a fixed distance D of 400 pixels. In part A (“target incomplicant”), W was fixed at 20 pixels. Participants performed under the five sets of strategy instructions as in Experiment 3 (EA, A, N, F, EF). Under each instruction set, they performed 14 trials. There was a total of 700 trials collected (= 5 instructions x 14 trials x 10 participants). No accidental trials were observed. The goal of part A was to produce a set of time measurements under the same nominal target width, but very different effective target width W_e due to different levels of target width utilization. Based on the experience of Experiment 3, I_u was about -1, -0.5, 0, 0.5 and 1 bits in EA, A, N, F and EF bias conditions, respectively, which map 20 pixels (W) to five different W_e values to approximately 10, 14, 20, 28 and 40 pixels.

In part B (“target compliant”), W was set at 10, 14, 20, 28 and 40 pixels, corresponding to the expected W_e values in part A. The goal of Part B was to produce a set of time measurements when participants obediently complied with the given target widths to an (almost) ideal extent: the $|I_u|$ value should be less than 0.1 bit (i.e. W_e matches W within 7% margin). To achieve that, we used a target width enforcement method inspired by and refined from the verbal feedback method of Guiard and colleagues (Zhai et al., 2003). During the experiment (after the first 5 trials in each block), if the running I_u value was greater than 0.1 (i.e. $W_e > 1.072W$), which meant that the participant took too much risk, a sign appeared in the middle of the two target strips to remind the performer to slow down. In contrast, if I_u was less than -0.1 (i.e. $W_e < 0.933W$), a sign of different color appeared to remind the participant to speed up. If no sign was displayed, it meant the participant's current endpoints dispersion corresponded to W within a 7% margin so the participant could keep his or her current pace.

The method of measuring the running I_u (W_e) value was as follows: Before the participant performed the 15th trial in a W condition, the program calculated the standard deviation of the endpoints distribution based on all of the past trials (from 1 to 14). From the 15th trial the program calculated the standard deviation of the endpoints, based on the most recent 14 trials (i.e. a 14-trial moving window was used). The experiment program stopped the current W condition and began the next one once a block of 14 trials whose $|I_u|$ value was less than 0.1 was captured (i.e. their W_e matched W by a less than 7% margin). These 14 trials were used in later analysis. The program would have also aborted the current W condition if the participant had performed 30 trials without reaching a 14 trial block that met the requirement. In the actual experiment, none of the participants needed to use up the maximum 30 trials. We analyzed the endpoints of the last 14 trials and confirmed that they were normally distributed. The standard deviation calculation was

based on the distance of the endpoints to the center of their distribution, not the center of the target (Isokoski and Raisamo, 2002). The order of the W condition was randomized in our experiment.

Therefore, through part A, we could observe the relationship between mean trial completion time and the effective target widths under different levels of target utilization as a result of the participants' disrespect of the nominal target width to varying directions and extent. Through part B, we could observe the relationship between mean trial completion time and the nominal target width when the participants obediently and effectively complied with the accuracy tolerance specified by the target. Comparing the *target width compliant scheme* and the *target width in compliant scheme* we could directly examine whether and how well W_e reconciles the two layers of speed-accuracy trade-off.

6.2 Results

Table 9 shows the results of Experiment 4. Figure 12 (left) shows the logarithmic regression results from the two experiment schemes (Part A and B). Figure 12 (right) show the Fitts' law regression of Part A and Part B, using I_{de} and I_{dn} respectively. The two sets of scatter plots (and regression lines and curves) show that the relationship between completion time and W_e in the target in compliant scheme (part A) and the relationship between completion time and W in the target compliant scheme (part B) were consistent in direction, but different in extent. In the near-zero range of I_u ($< |0.5|$ bits, or $W/2^{0.5} < W_e < W/2^{-0.5}$), the difference was relatively small. When I_u was beyond such a range, this difference increased rapidly. The greater $|I_u|$ was, the greater such a difference was.

part A		EA	A	N	F	EF
	W	20	20	20	20	20
	error %	0	1.4	4.2	17.8	25
	W_e	9.54	14.98	18.20	30.58	37.69
	time	992.5	797.2	634.4	593.3	489.2
part B	W	10	14	20	28	40
	W_e	11.03	14.54	21.90	30.96	44.36
	time	860.8	744.8	639.2	611.8	526.8

Table 9. Results of Experiment 4

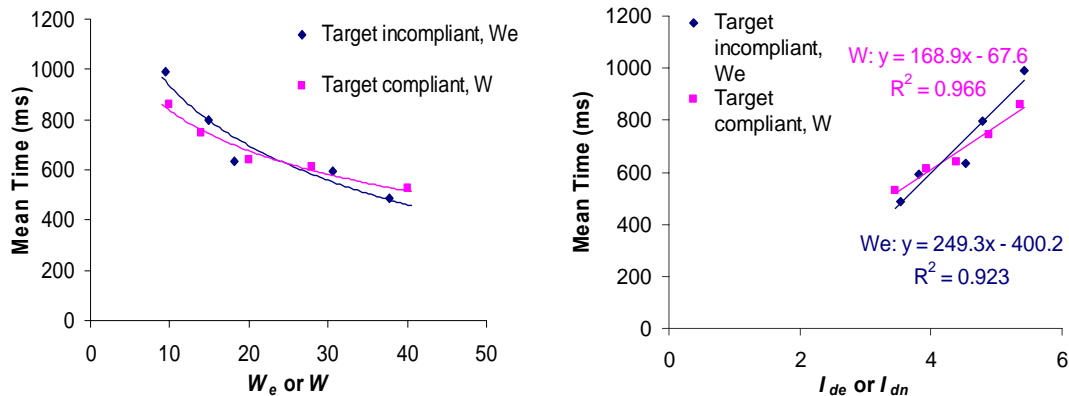


Figure 12. The match between T vs. W_e in the target inconcompliant scheme and T vs. W in the target compliant scheme (left) and their corresponding Fitts' law regressions (right)

The results of this experiment shed more light on the effect that I_{de} only partially compensates for the time variance caused by different operating biases (different target utilization levels): while the T vs. W_e relationship in the presence of I_u variance was similar to T vs. W relationship when the performers obediently complied with the target width specification (with no or little I_u variance), they did not exactly match in extent. The impact of the W_e adjustment lagged behind the impact of W changes in the same amount.

7. Further Analyses

The foregoing analyses clearly indicate that the use of W_e is an imperfect and insufficient adjustment of W to overcome I_u variances in Fitts' law tasks, although the direction of adjustment was empirically correct. Is it possible to find an adjustment that more fully compensates the impact of I_u variance? Given that W_e under-corrects when the endpoints dispersion deviated significantly from the nominal width W (shown in Figure 12), a more exaggerated effective width could possibly account for more of the remaining difference in completion time. This suggests the following modified effective width is worth investigating:

$$W_m = W \left(\frac{W_e}{W} \right)^\alpha \quad (9)$$

i.e.

$$W_m = W \left(\frac{4.133\sigma}{W} \right)^\alpha \quad (10)$$

Where σ is the standard deviation of the endpoints distribution.

α should be greater than 1 in order to cause W_m to nonlinearly exaggerate the impact of deviation from W : When W_e is close to W , W_m has a similar value to W_e ; When $W_e \gg W$ or $W_e \ll W$, W_m is much greater or much smaller than W_e . The greater the α value is, the more pronounced difference there is between W_m and W_e . When α is 1, W_m reduces to W_e .

Accordingly,

$$I_{dm} = \log_2 \left(\frac{D + W_m}{W_m} \right) \quad (11)$$

and

$$T = a + bI_{dm} \quad (12)$$

Based on the empirical data from Experiment 4, 1.5 is a good estimate of α . Figure 13 (left) shows the mean trial completion time as a function of W_m with $\alpha = 1.5$ (the target inconcompliant condition of Experiment 4). The relationship between time and W_m matches almost exactly the relationship between time and nominal W when participants closely obeyed the target width (the target compliant condition of Experiment 4). Figure 13 (right) shows the corresponding Fitts' law regressions using I_{dn} and I_{dm} .

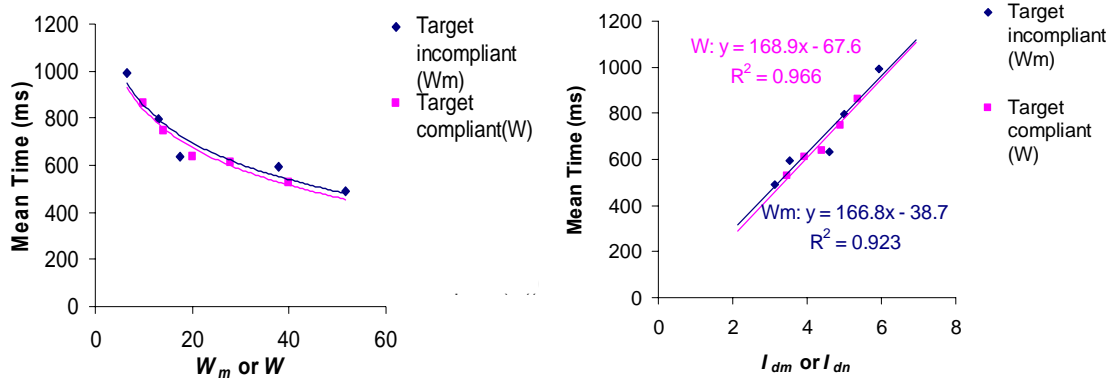


Figure 13. The match between T vs. W_m in the target in compliant scheme and T vs. W in the target compliant scheme (left) and their corresponding Fitts' law regressions (right)

Of course, the value of α based on one small experiment (Experiment 4) is not likely to be an accurate estimate for other data sets, although it is plausible that a better compensation may be achieved by W_m with certain α value. A potential difficulty that W_m faces, however, is the limitations of W_e adjustment that we see in the first three experiments: while the W_e adjustment reduced the discrepancy of Fitts' law coefficients measured under different operating biases, it also weakened the strong regularity within each operating condition as modeled by $T = f(I_{dn})$. Since W_m is a more exaggerated version of W_e , the correlation of T vs. I_{dm} may be reduced further from that of T vs. I_{dn} within each operating condition. Another obvious weakness of the notion of W_m is that since it is based on W , W_e and another parameter α , its direct definition is lacking or to be discovered in the future.

To test the possibly stronger compensation power of W_m and its likely drawbacks, we reanalyzed the first three experiments, substituting I_{de} with I_{dm} (with $\alpha = 1.5$). The results are summarized in Figures 14 to 16 and Table 10.

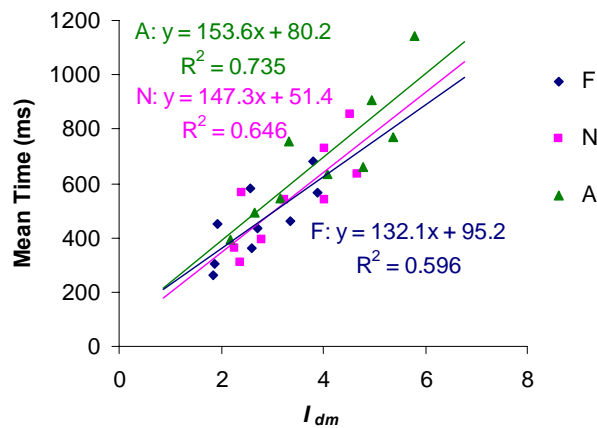


Figure 14. T vs. I_{dm} regression of Experiment 1 (Compare with Figures 3, 4)

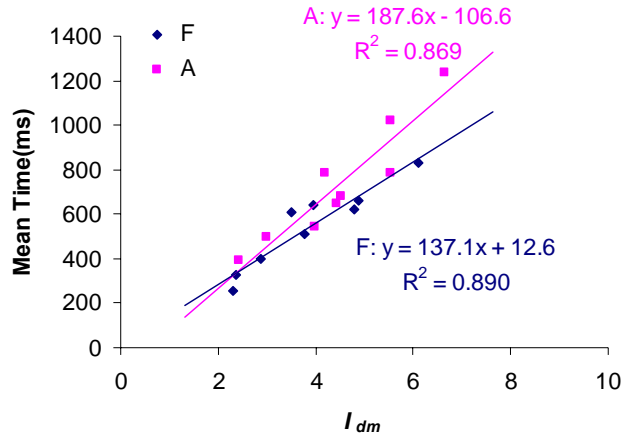


Figure 15. T vs. I_{dm} regression of Experiment 2 (Compare with Figure 6)

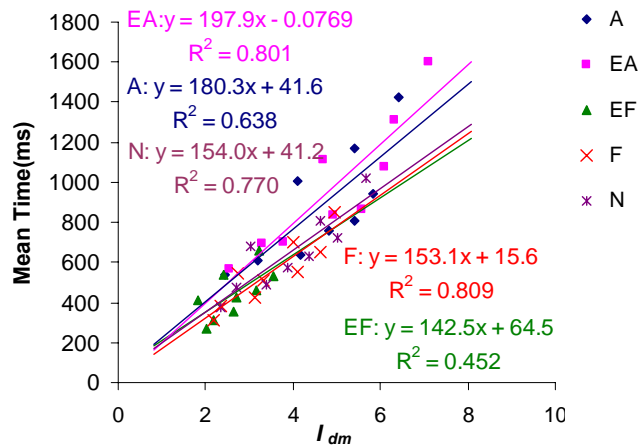


Figure 16. T vs. I_{dm} regression of Experiment 3 (Compare with Figure 7)

1	2	3	4	6	7	8	9	10
	I_a	EA	A	N	F	EF	Mixed	
		a, b, r^2	a, b, r^2	a, b, r^2	a, b, r^2	a, b, r^2	a, b, r^2	$\Delta b/b_{min}$
Expt 1	I_{dn}		161, 150, 0.95	123, 118, 0.98	123, 92.4, 0.99		135, 120, 0.70	49%
	I_{de}		92.7, 156, 0.83	41.5, 147, 0.84	56.1, 133, 0.87		13.2, 161, 0.83	16%
	I_{dm}		80.2, 154, 0.73	51.4, 147, 0.65	95.2, 132, 0.60		38.3, 157, 0.75	15%
Expt 2	I_{dn}		111, 173, 0.93		111, 119, 0.92		111, 146, 0.75	45%
	I_{de}		-28.1, 182, 0.90		48, 131, 0.91		76.2, 141, 0.60	39%
	I_{dm}		-107, 188, 0.87		12.6, 137, 0.89		-80.9, 172, 0.85	37%
Expt 3	I_{dn}	201, 215, 0.90	210, 186, 0.90	171, 131, 0.96	141, 113, 0.996	138, 83.8, 0.99	172, 146, 0.46	100%
	I_{de}	63.6, 204, 0.84	76.0, 187, 0.75	75.8, 149, 0.87	45, 143, 0.93	7.5, 147, 0.88	-92.4, 208, 0.78	41%
	I_{dm}	-0.08, 198, 0.80	41.6, 180, 0.64	41.2, 154, 0.77	15.6, 153, 0.81	64.5, 143, 0.45	-82.1, 199, 0.81	36%

Table 10. Comparison of I_d , I_{de} and I_{dm} in Experiment 1, 2 and 3; highlighted is the most neutral condition in each experiment (cf. Table 6).

Based on the degree of convergence of the regression coefficients (see Column 10 of Table 10), I_{dm} compensates for the different levels of I_u slightly better (Experiment 1, Experiment 2) or better (Experiment 3) than I_{de} . Taking the b value in Experiment 3 (the most comprehensive and balanced experiment) as an example, under the EA, A, N, F, EF operating conditions b was 215, 186, 131, 113, 83 ms/bit with I_{dn} ; and 204, 187, 149, 143, 147 ms/bit with I_{de} . With I_{dm} , b was 198, 180, 154, 153, 143 ms/bit. If we use the estimates under Condition N as the best possible estimate, the b values can be written as percentage changes from its best estimate, as shown in Table 11. I_{dm} appears to offer better correction of operating biases than I_{de} (See also Figure 16 in comparison to Figure 7).

	EA (%)	A (%)	N (base)	F (%)	EF(%)
I_{dn}	64.1%	42%	131	-13.7%	-36%
I_{de}	36.9%	25.5%	149	-4 %	-1.3%
I_{dm}	28.6%	16.9%	154	-0.6%	-7.1%

Table 11. b estimate as percentage variation from the neutral condition (N) in Experiment 3

However, the limitations of I_{dm} were also apparent. First, it still could not completely compensate for the speed accuracy tradeoff caused by different levels of target utilization. The coefficients measured under different operating biases still did not fully converge. Second, since W_m is a nonlinear amplification (or reduction) of W_e , it weakened the regularity found in T vs. I_d even more than W_e , as indicated by the further decreased r^2 values within each condition (Table 10). When mixing all biased conditions, the r^2 of T vs. I_{dm} was similar to the r^2 of T vs. I_{de} : weaker in Experiment 1, but stronger in Experiments 2 and 3.

One could argue that stronger results with I_{dm} could be achieved with different α values. As Table 12 shows, this was indeed true, but there was not a α value that is optimal for all experiments with different ranges and sets of operating biases.

	$\alpha=1.2$			$\alpha=1.3$			$\alpha=1.5$			$\alpha=1.8$		
	a	b	r^2	a	b	r^2	a	b	r^2	a	b	r^2
EXP. 1	13.9	162.1	0.808	19.0	161.3	0.792	31.2	157.9	0.745	86.2	144.1	0.656
EXP. 2	-44.6	168.4	0.835	-57.1	169.8	0.839	-80.9	172.43	0.845	-113.1	175.3	0.849
EXP. 3	-100.7	207.3	0.806	-98.2	205.4	0.811	-82.1	198.8	0.807	-37.4	184	0.778

Table 12. Regression results with mixed conditions at different α values

Mathematically, the α term in Equations 9 —12 can be separated from I_{dn} . Considering that D is typically greater or much greater than W , and when W_e/W is not too distant from 1, the following equation approximates Equation 12:

$$T = a + b \log_2 \left(\frac{D+W}{W} \right) - b\alpha \log_2 \left(\frac{W_e}{W} \right) \quad (13)$$

or

$$T = a + bI_d - b\alpha I_u \quad (14)$$

or

$$T = a + bI_d + cI_u \quad (15)$$

where $c = -ba$.

Multiple regression results (a , b , and c) based on the first three experiments, however, tended to be highly dependent on which experimental conditions were included in the regression, suggesting the complex interactive nature of the I_{dn} and I_u effect.

Figure 17 shows the mean of the completion time T as a function of I_{dn} and I_u based on data from Experiment 3 (all conditions mixed). As we can see, while T increased with I_{dn} and decreased with I_u , in general, they did not form a strictly monotonic function, suggesting complex interaction effects between I_{dn} and I_u . This means that it is difficult, if not impossible, to establish a model that captures both layers of speed-accuracy tradeoffs in a complete and yet simple (linear) manner.

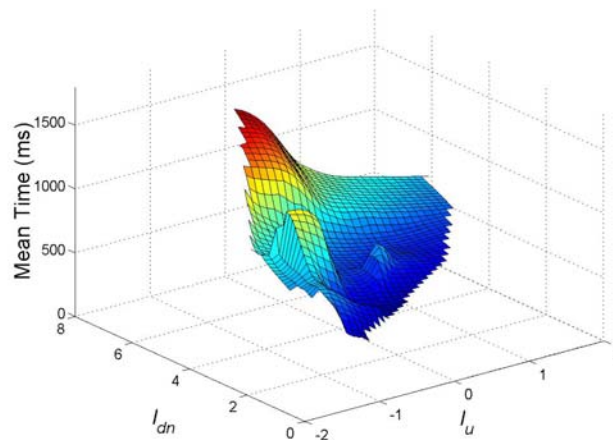


Figure 17. 3D perspective illustration of $T = f(I_{dn}, I_u)$ based on data from all conditions in Experiment 3

8. General Discussion and Conclusions

We have systematically explored the two layers of speed-accuracy trade-off in Fitts' aimed movement tasks. Fitts' law in its original form reveals the speed-accuracy tradeoff relationship between pointing completion time and task precision based on the nominal, objective, geometrical parameters of the target (D and W). However, in actuality speed-accuracy relationship in pointing also contains another subjective layer which depends on how obediently the performer complies with the specified target width and what bias the performer takes (toward either accuracy or speed). This performer introduced accuracy layer causes a discrepancy between the nominal task precision and the actual behavior precision. We defined an index of target utilization, $I_u = \log_2(4.133\sigma/W)$, to quantify the degree of this mismatch. As is implicitly realized in the Fitts' law literature, and as this study has explicitly and systematically shown, Fitts' law tasks tend to involve both layers of speed-accuracy tradeoffs. Our study shows I_u is never constant in an experiment, even within the same instruction set, such as "as accurately as possible and as fast as possible," except when an enforcement method is applied, as in Experiment 4. The overall I_u level can be influenced by the experimental instruction in the laboratory, or by performers' preference and task strategy in real world tasks.

This study clearly demonstrated that varied I_u values influence Fitts' law regression modeling, resulting in different a b coefficients which in the context of human-computer interactions are often used to characterize an input system's efficiency. The classic approach to correct the influence of varying I_u is the so-called "effective target width" method. This approach takes the performer's actual behavioral parameter, W_e , rather than the nominal target width W , as the basis of index of difficulty calculation. Such an approach has not had a strong theoretical or empirical foundation in the literature.

In a set of four experiments, we deliberately manipulated I_u over a wide range or controlled to specific levels through instructions and feedback control, which enabled us to investigate the two layers of speed-accuracy tradeoff systematically. Our investigation has led to the following conclusions.

First, the task form of Fitts' law $T = f(I_{dn})$ is a very strong model. The nominal I_{dn} is an impressive determinant of mean movement time, accounting for up to 99% time variance within an experimental condition. Revisions of index difficulty to a behavior form, either through W_e , or its more aggressive version W_m , consistently weaken the regularity within an particular operating bias condition. On the other hand the resulting coefficients of T vs. I_{dn} can be easily swung by I_u levels. In the context of HCI, this poses a serious challenge to assessing the quality of various input systems (Zhai, 2004).

Second, I_{de} partially incorporates the second, subjective accuracy layer into Fitts' law model by adopting an actual and behavior parameter W_e . The first three experiments showed that adopting W_e reduced the discrepancy of a and b estimates between different experimental conditions. Experiment 4 shows that, although not completely congruent, the impact of the *a posteriori* effective target width was similar to that of *a priori* nominal target width with which the performer obediently complied. The compensation effect of W_e was also shown by the higher r^2 value of T vs. I_{de} regression across different operating biases (mixed data from all conditions) than the r^2 value of T vs. I_{dn} regression. This study, to our knowledge, provided the first systematic empirical foundation for the use of W_e . However, the compensation effect of W_e is gained at the cost of weakened regularity within each experimental condition.

Third, I_{dm} , the more aggressive version of I_{de} , takes a step further than I_{de} in both I_{de} 's pros and cons: it more fully compensates for the I_u impact but further weakens regularity within each operating strategy condition.

Fourth, in the absence of the subjective layer of speed-accuracy tradeoff (the performer completely complies with task specification, keeping I_u at or near zero), both I_{de} and I_{dm} revert to the nominal I_{dn} . In that sense, no harm can be done by adopting I_{de} and I_{dm} .

Fifth, the level of target utilization in Fitts' law tasks, as measured by the index of target utilization $I_u = \log_2(W_e/W)$, can be influenced by three factors: the overall operating bias (in the lab by instruction, in reality by user's strategic choice); nominal target W ; and target distance D . However, W and D have very different degrees of impact on I_u , with the former being far greater than the latter. This means that the change from I_{dn} points (determined by D and W) to I_{de} points (determined by D and W_e) is not uniform. Given that T and I_{dn} forms a very strong correlation within each strategy, the use of I_{de} or I_{dm} would only weaken this correlation. A compromise has to be made between the goodness of fit within each condition and better estimates of a and b . Fundamentally, the use of I_{de} or I_{dm} is to incorporate a different layer of speed-accurate tradeoff (the subjective layer) into a very strong time and task accuracy relationship as modeled by $T = f(I_{dn})$.

Sixth and finally, the two layers of speed accuracy tradeoff in pointing interact in a complex manner. They do not cause a simple additive effect, hence the difficulty of using $T = f(I_{de})$ or $T = f(I_{dm})$ and any other potential relationship as a strong general model.

In summary, this systematic investigation reveals the nature and the relationship of speed and accuracy in pointing. The implication of this study depends on the specific purpose of use. Theoretically we now know that the two layers of speed-accuracy tradeoffs, the objective and task layer and the subjective and behavior

layer have different impact on task performance. The impact of actual pointing precision W_e and the impact of nominal pointing precision W are not equivalent, but are numerically similar, particularly when W_e is not too distant from W . The findings in this work also have more general implications to human motor control theory. One of the central issues in early motor control literature was the closed-loop vs. open-loop nature of human motor skills (Stelmach, 1976). This study shows that even for a low level tapping task, both external visual feedback and internal bias settings contribute to the control process. In a manual stabilization task, Pew (1966) showed that humans not only react instantaneously to the position of a controlled object, but can also adjust higher level control parameters to achieve stabilization. This experiment shows that in pointing tasks performers could adjust their overall bias towards speed or accuracy and integrate such an internal high level setting with the external low level visual feedback to manage a pointing process.

Practically, the findings in this study suggest that in order to accurately measure Fitts' law parameters, I_u should be kept as close to zero as possible and its variance should be kept as low as possible. One possible method of controlling I_u in Fitts' law studies is to use endpoints standard deviation-based feedback, as we did in Experiment 4. When I_u is highly varied or when it is not near zero, however, this study provides an empirical foundation for the application of W_e or its more aggressive and more complete version, W_m , to adjust for I_u changes. These adjustments consistently yield more logical Fitts' law parameter estimates, a and b , although one should also be aware of the limitations and side effects of W_e or W_m , including reduced correlation between pointing time and index of difficulty within each operating strategy and their incomplete compensation for the subjective layer of speed-accuracy tradeoff.

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